

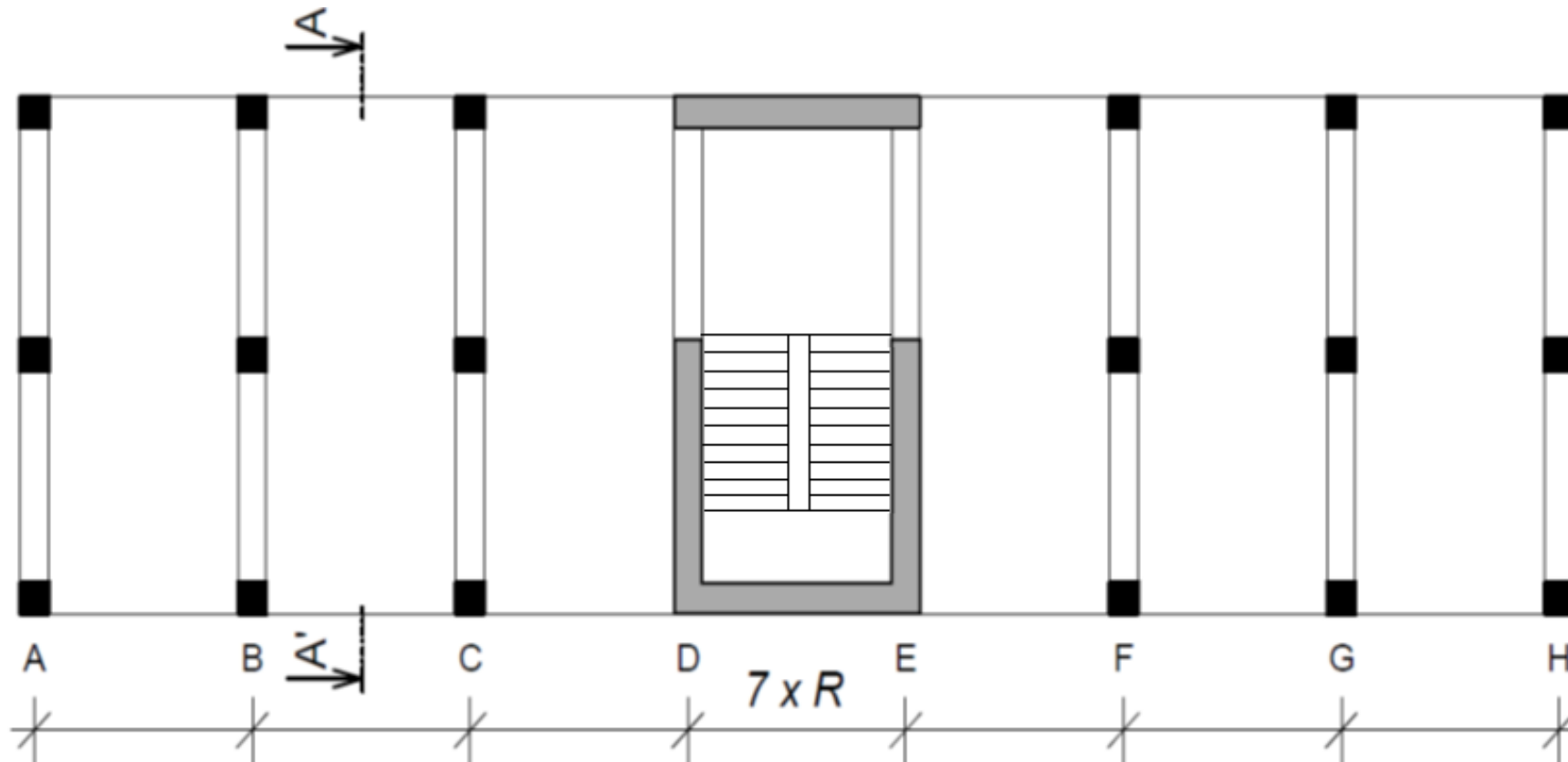


CM01 – Concrete and Masonry Structures 1
HW10 & HW11 – Staircase

Task 5

Task 5 – Staircase

In Task 5, **reinforced concrete staircase** will be designed into the structure from Task 1.



Task 5 – Assignment

Task 5: Reinforced concrete staircase

Design a staircase for the structure from Task 1. Staircase will be supported by the reinforced concrete core. Adjust the span of the core if necessary (the distance between axes D and E need not to be equal to R).

Please work out:

1. **Design of dimensions of a reinforced concrete staircase** (including details of flight-landing connections)
2. **Design of staircase reinforcement.**
3. **Sketch of staircase reinforcement.**
4. **Structural drawing** of a part of the structure from Task 1 with the designed staircase in 1:25 scale.

Task 5 – Assignment goals

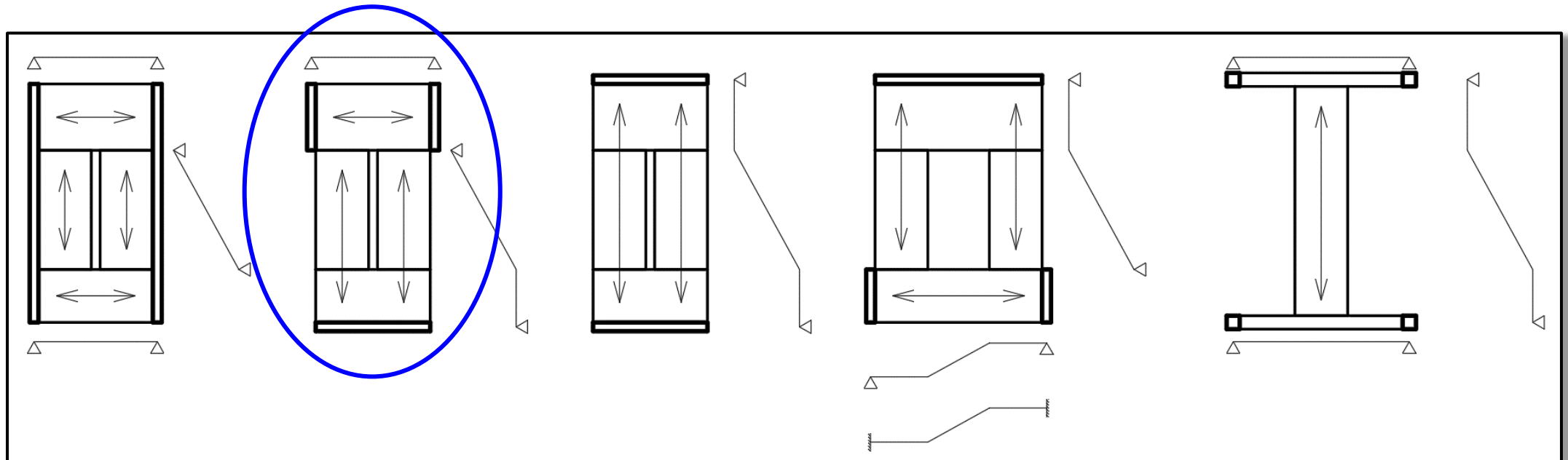
Our goal will be to:

- 1) Design the **geometry** of the staircase.
- 2) Calculate **loads** and bending **moments**.
- 3) Design the **reinforcement**.
- 4) Sketch a **drawing** of the reinforcement.

Conceptual design

Conceptual design

In general, there are usually **many possibilities** how to design the staircase. This **presentation describes just one possible approach** for our particular structure.



Geometry

Geometry

The specific geometry of the staircase is up to you. However, the design must be done according to **staircase design rules**:

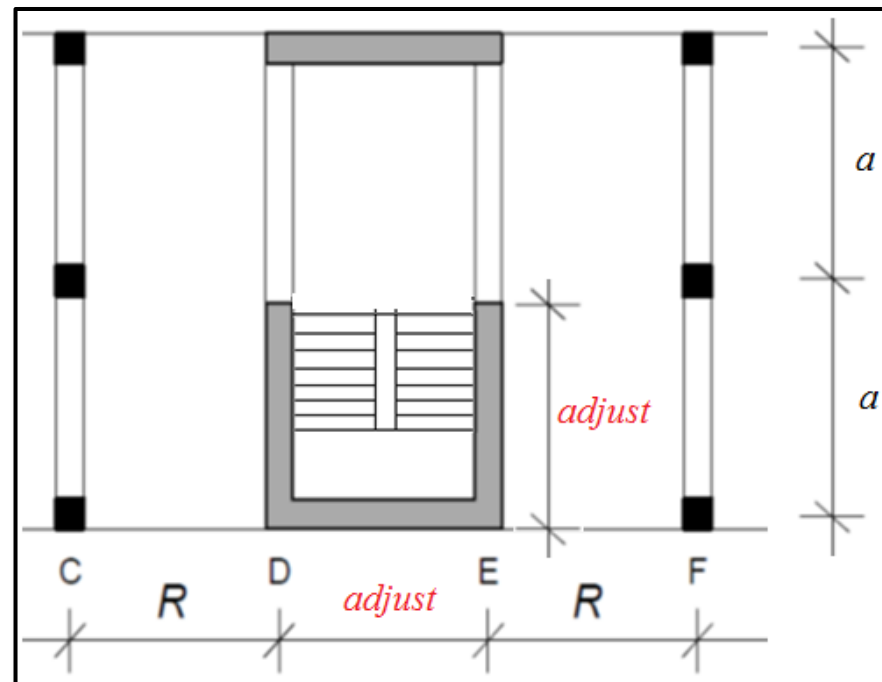
- dimensions of a step must satisfy: $b_{step} = 630 - 2h_{step}$,
- maximal number of steps in one flight: 16,
- minimal width of the flight: 1100 mm,
- minimal width of the landing: 1100 mm,
- minimal the gap between the flights: 200 mm,
- minimal perpendicular clearance: $750 + 1500 \cdot \cos\alpha$,
- minimal head clearance: $1500 + 750/\cos\alpha$.

Follow the [example](#) on my webpage.

Geometry

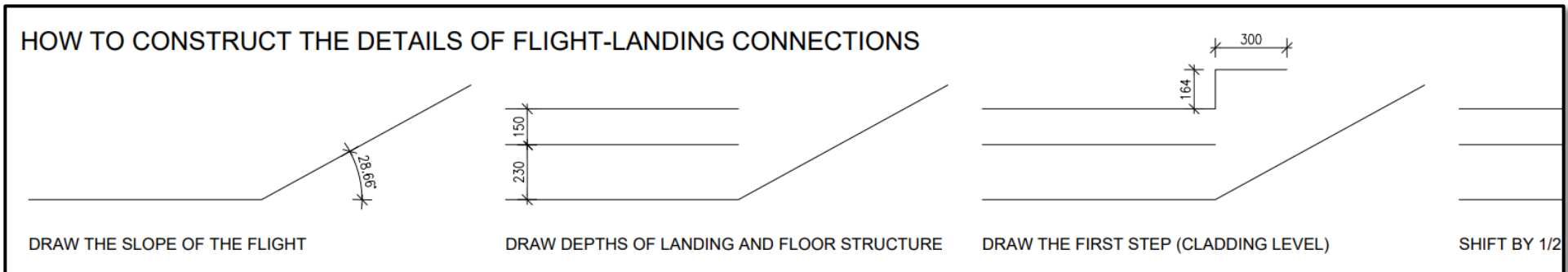
Design the staircase and **draw a scheme of the staircase.**

If needed, **you can adjust the dimensions of the supporting walls** according to your staircase geometry.



Geometry of flight-landing connection

Geometry of flight-landing is already given by the designed geometry! We have to **adhere to the designed geometry when drawing the connection.**

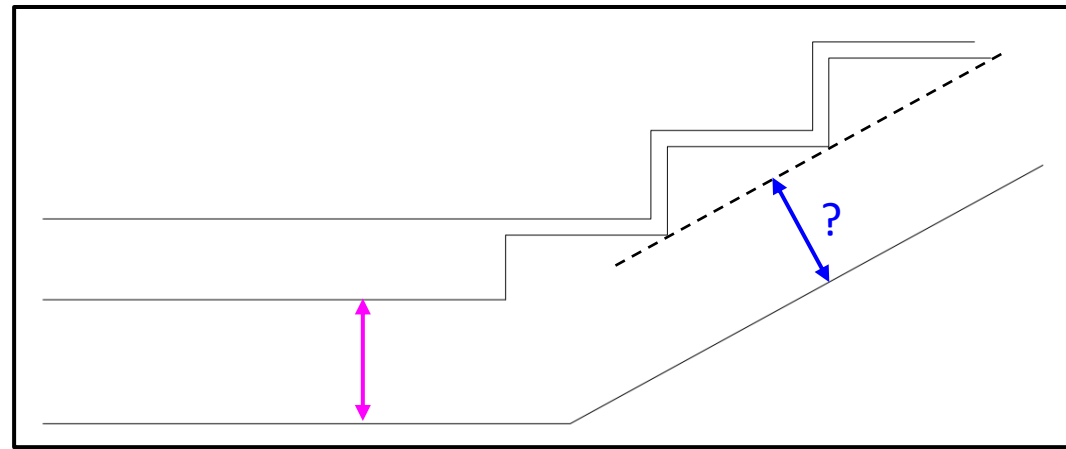


See the [guide for connection drawing](#).

Geometry of flight-landing connection

Why do we draw the flight-landing connection?

To find the **exact thickness of the flight** for our given **thickness of landing** (see slab thickness in Task 1).

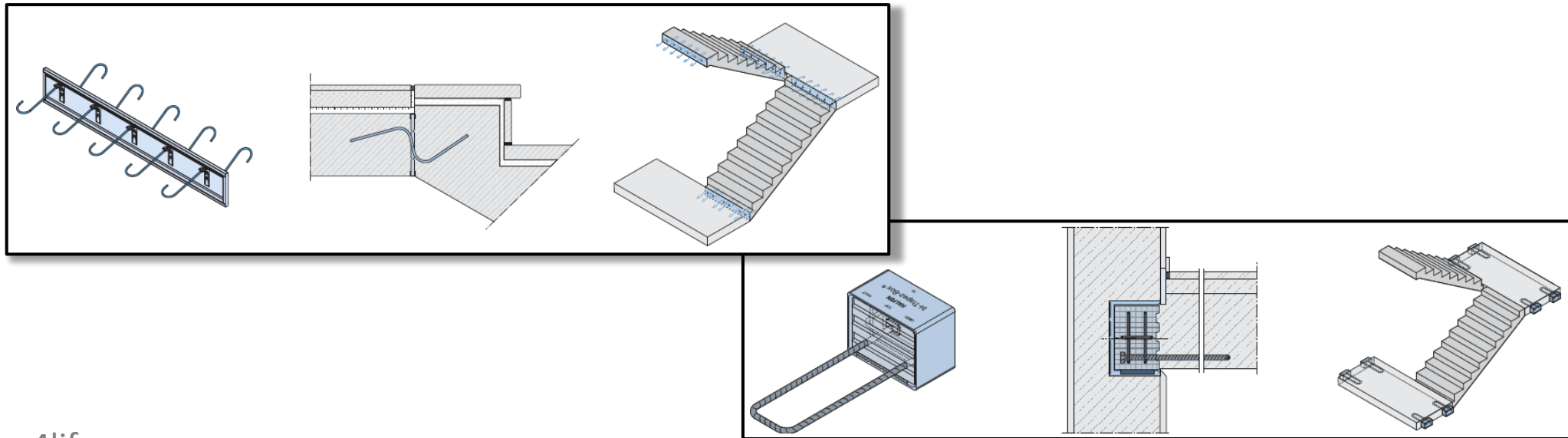


Supports

Supports

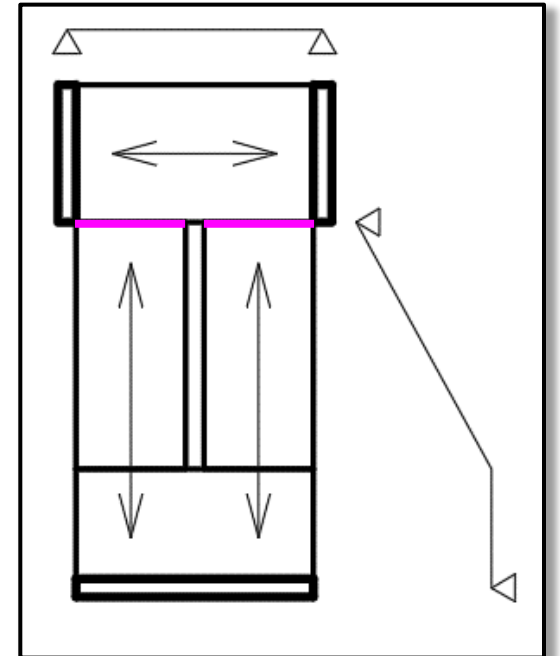
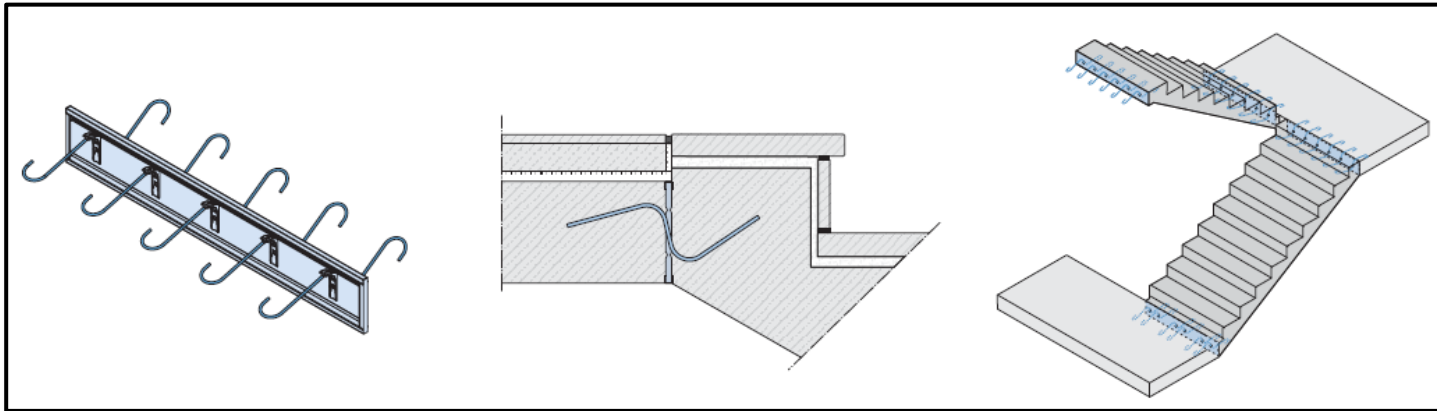
After the geometry of the staircase is designed, we must **determine how the staircase will be supported.**

The staircase will be connected with the supporting members by **special elements to prevent transfer of impact sound** to the rest of the building.



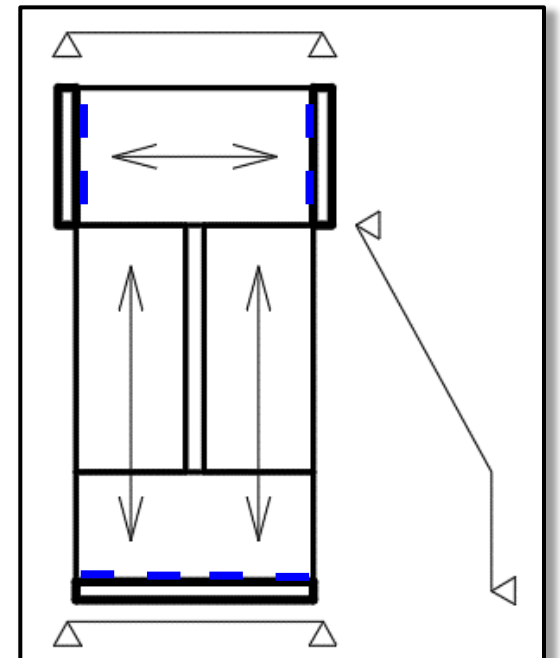
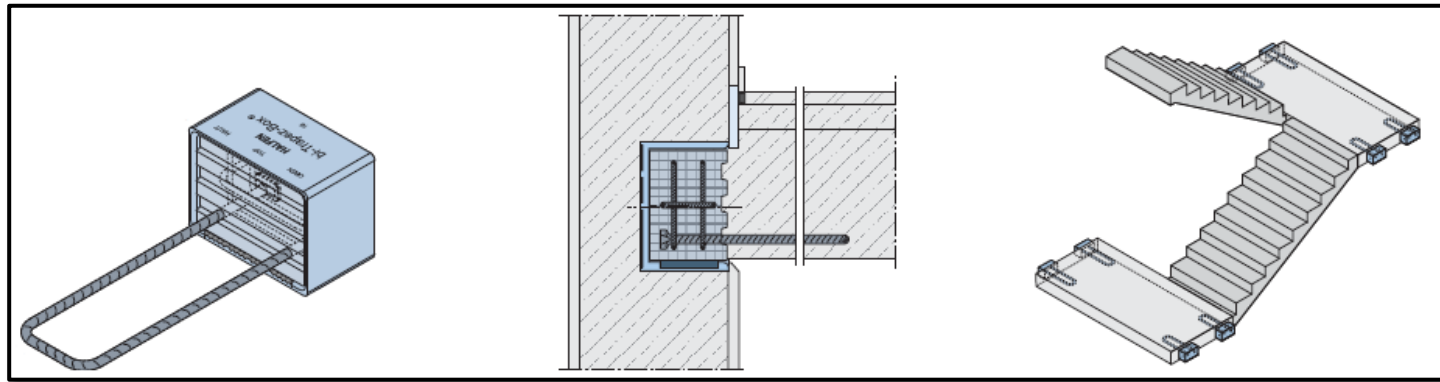
ISI unit

The **ISI units** are used for the connection between **flight and transversal landing**.



Trapez boxes

The **trapez boxes** are used for the connection between **landing and wall**.



Loads

Loads

Following loads are acting on the landing:

- self-weight of the slab: $g_{0,k} = h_{slab} \cdot 25$,
- self-weight of floor structure: use $g_{floor} = 1 \text{ kN/m}^2$,
- live load: use $q_{floor} = 3.5 \text{ kN/m}^2$.


Following loads are acting on the flight:

- self-weight of the slab: $g_{0,k} = h_{slab,vertical} \cdot 25$,
- self-weight of the steps: $g_s = (h_{step,vertical}/2) \cdot 25$,
- self-weight of the cladding of the steps: use $g_{floor} = 0.5 \text{ kN/m}^2$,
- live load: use $q_{floor} = 3.5 \text{ kN/m}^2$.

Follow the [example on my webpage](#).

Loads

Landing			
Load	Char. value [kN/m ²]	γ	Design value [kN/m ²]
Slab	0,23 · 25	1,35	7,8
Floor	1	1,35	1,35
Live load	3,5	1,5	5,25


 $f_{dl} = 14,4 \text{ kN/m}^2$


N/m²,

Following loads are acting on the flight

- self-weight of the slab: $g_{0,k} = h_{sl}$
- self-weight of the steps: $g_s = (h_s)$
- self-weight of the cladding of the
- live load: use $q_{floor} = 3.5 \text{ kN/m}^2$

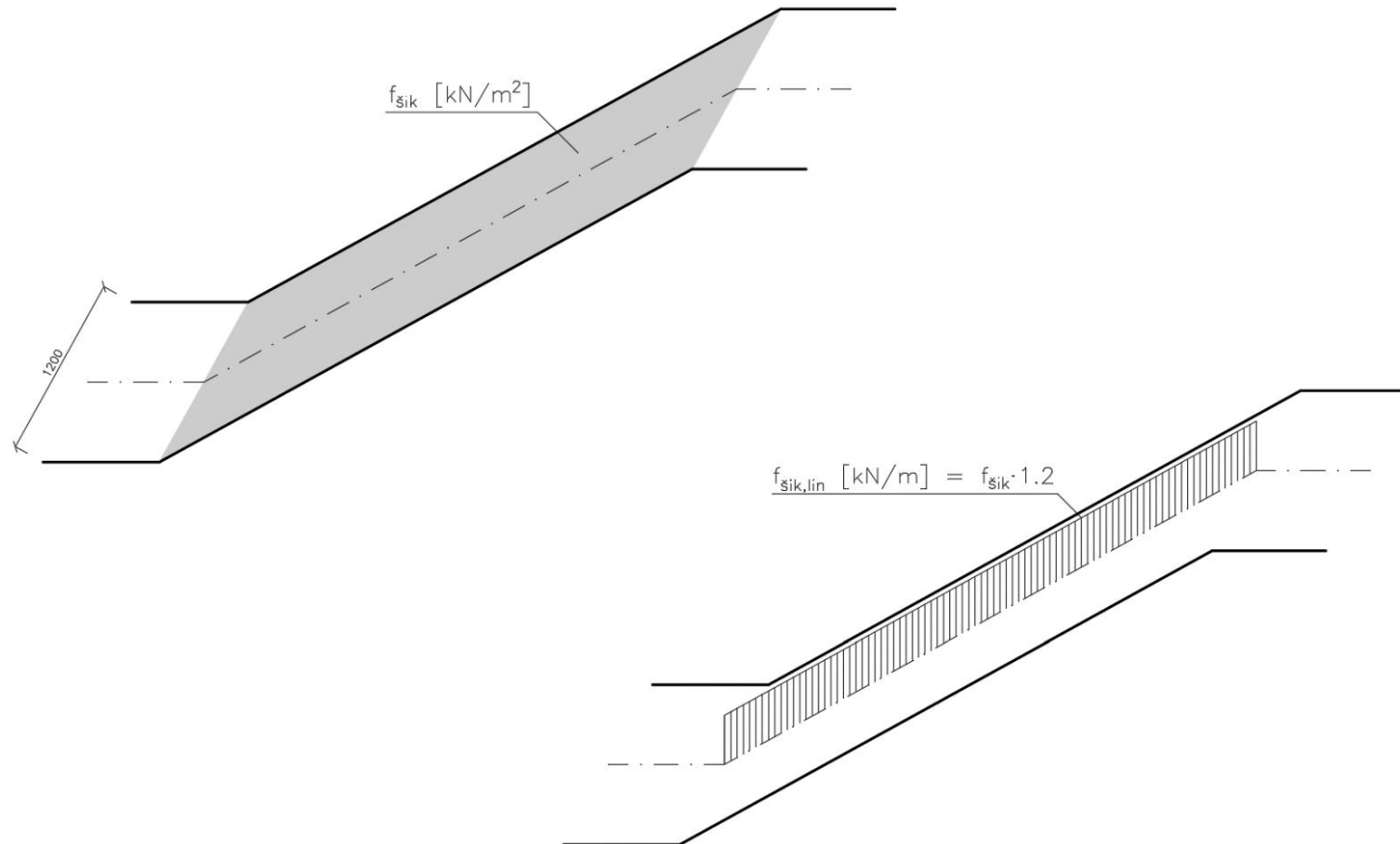
Follow the [example on my webpage](#)

Flight			
Load	Char. value [kN/m ²]	γ	Design value [kN/m ²]
Slab	$\frac{0,22}{\cos 28,66^\circ} \cdot 25$ ①	1,35	8,5
Cladding	$0,5 \cdot \frac{164+300}{300}$ ②	1,35	1,04
Steps	$\frac{0,164}{2} \cdot 25$ ③	1,35	2,78
Live load	3,5	1,5	5,25


 $f_{df} = 17,6 \text{ kN/m}^2$

Loads

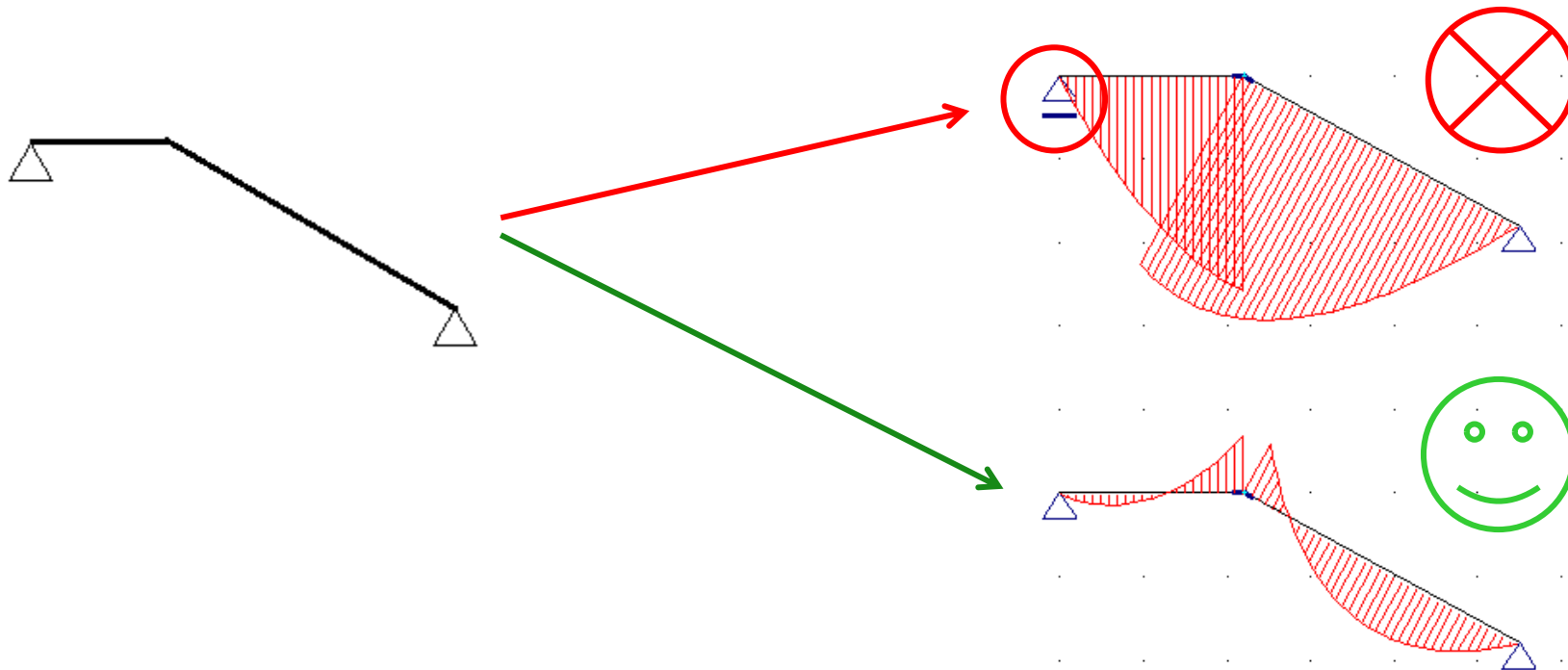
Finally, convert all area loads to **linear loads**!



Structural scheme

Structural scheme

The **supporting elements** that we selected **do not transfer bending moments**, and therefore, they act as **pinned supports**. Also, they **do transfer horizontal forces**!



Internal forces

Internal forces

The structure is **statically indeterminate** → we should use a **FEM program** or slope deflection method to calculate **real bending moments**.

However, we can make a **conservative (safe) estimation**:

$$m_{Ed} = \frac{1}{12} f_{df} l^2$$

Horizontal length of the staircase
(landing+flight)

Design load of stair flight or landing (use
the higher value) [kN/m]

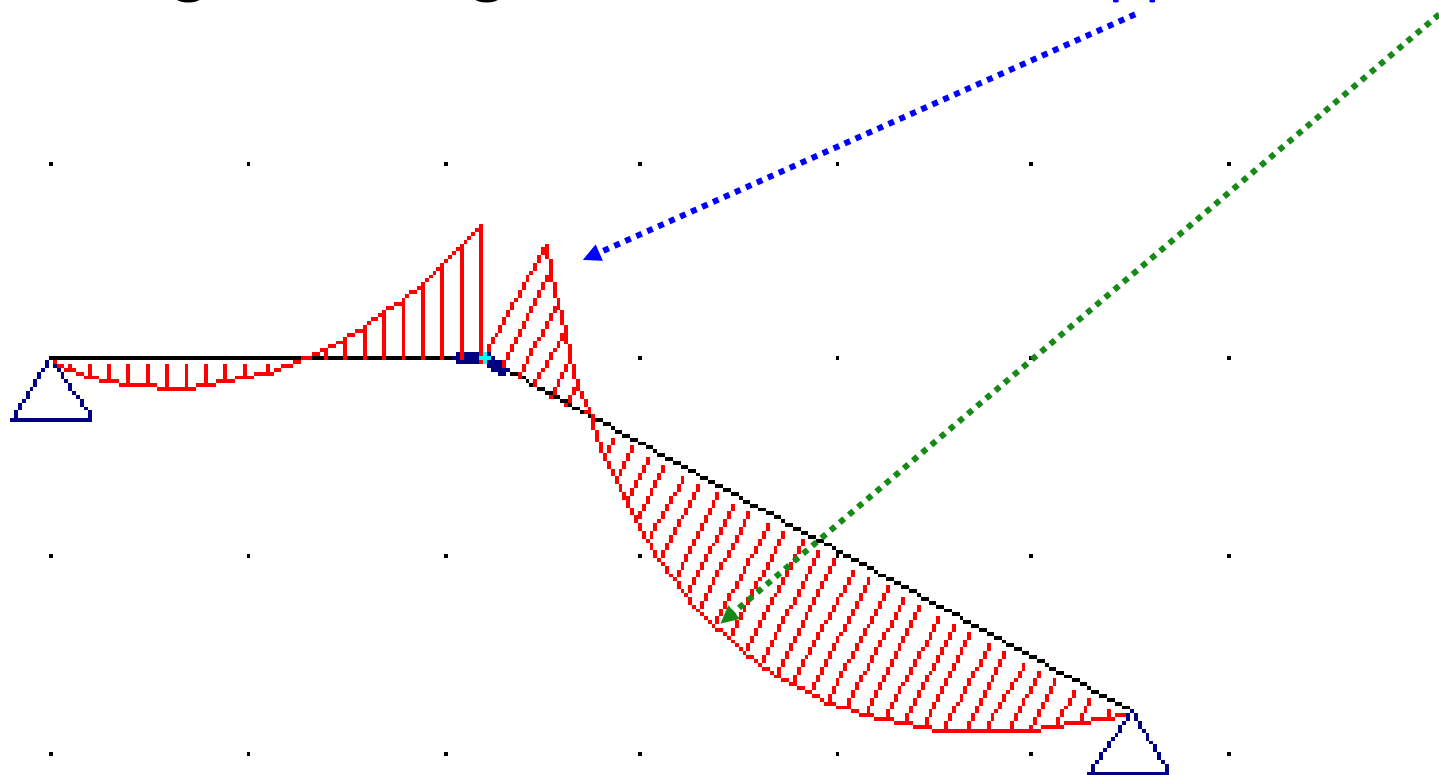
End of HW10

Start of HW11

Design of reinforcement

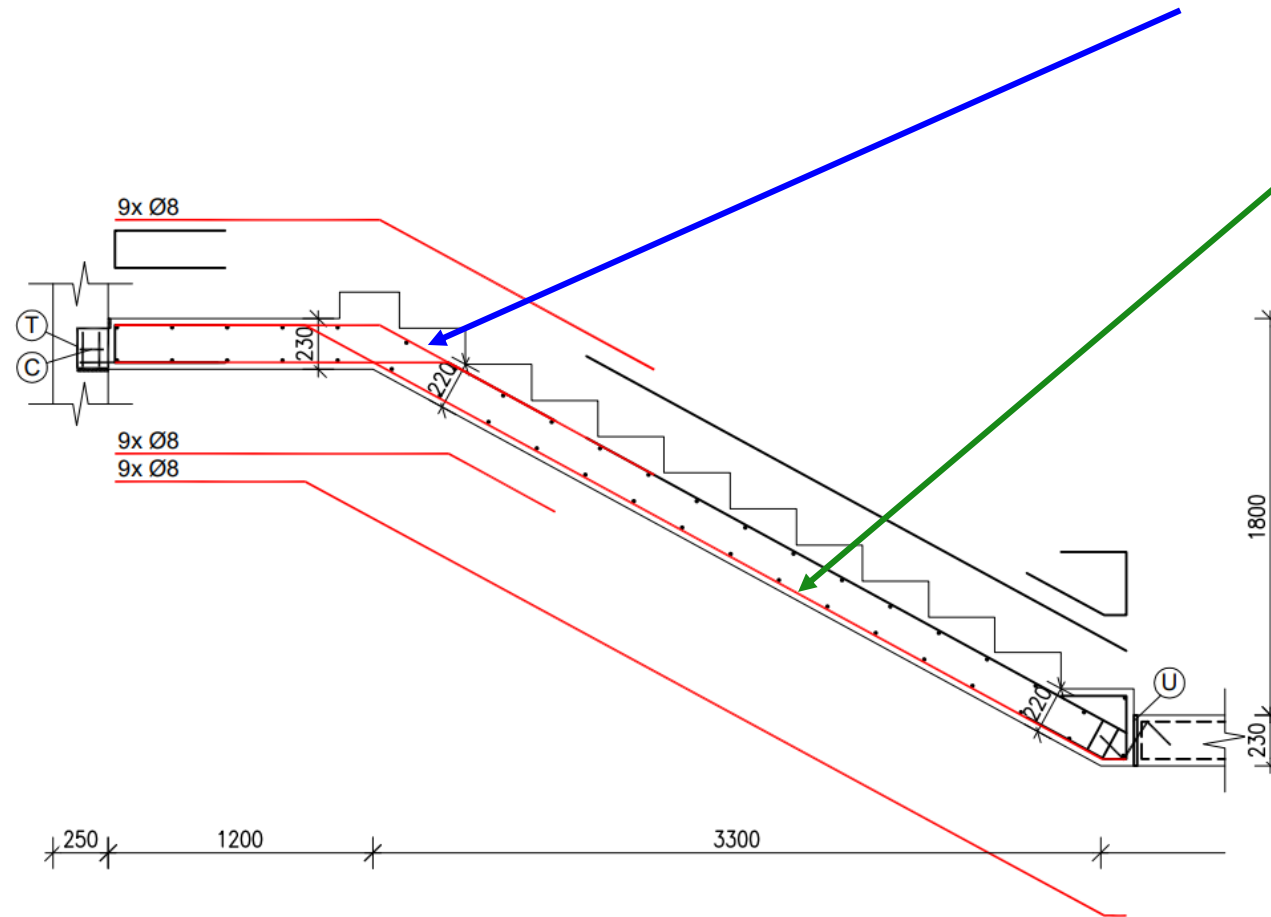
Design of reinforcement

Use the **estimated design bending moment** for both **upper** and **lower** main reinforcement.



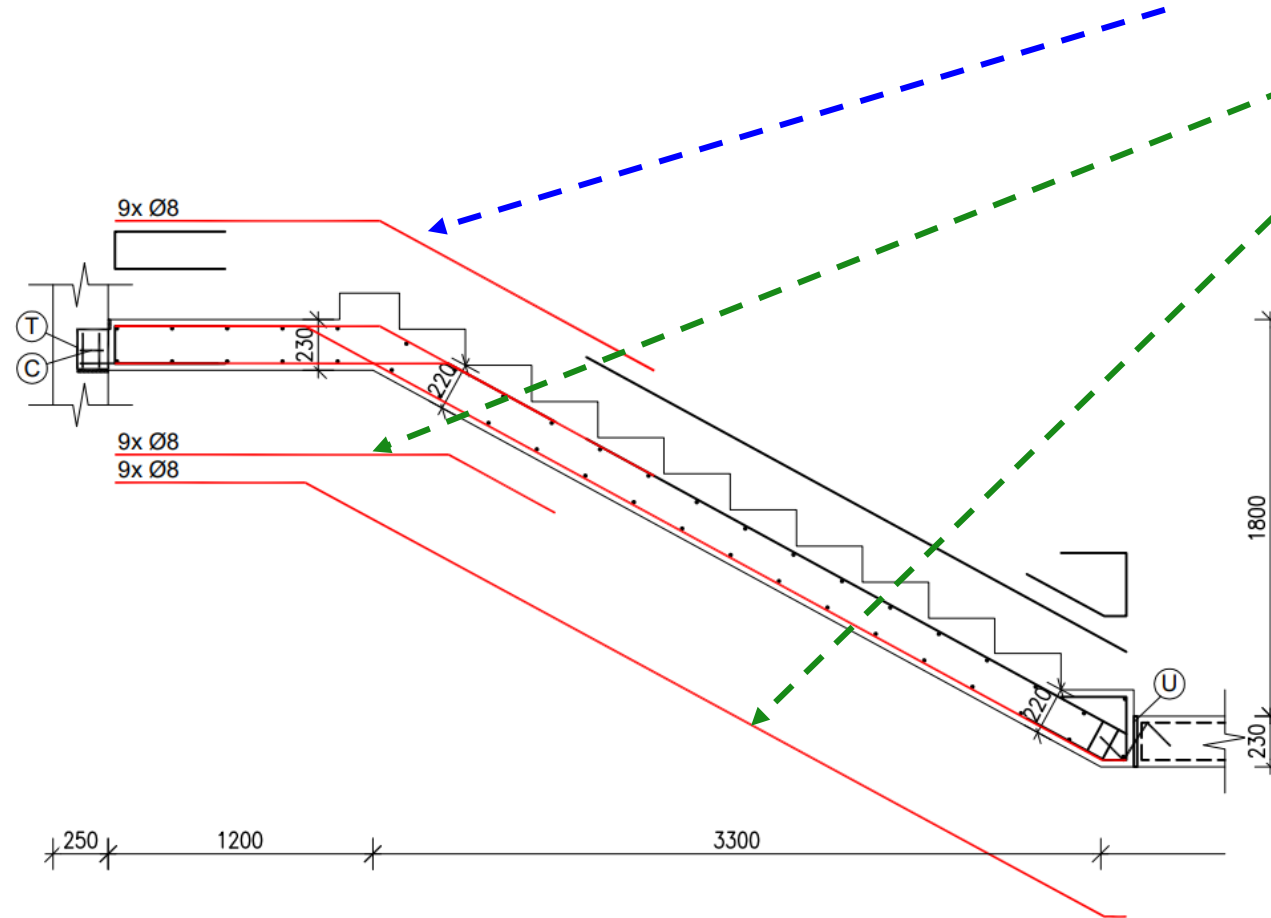
Design of reinforcement

Use the **estimated design bending moment** for both **upper** and **lower** main reinforcement.



Design of reinforcement

Use the **estimated design bending moment** for both **upper** and **lower** main reinforcement.



Design of reinforcement

Staircase is a one-way slab → **design of reinforcement is the same as for any other one-way RC structural member** (see HW3 and HW8):

$$A_{s,req} = \dots$$

$$A_{s,prov} = \dots$$

$$x = \dots$$

$$z = \dots$$

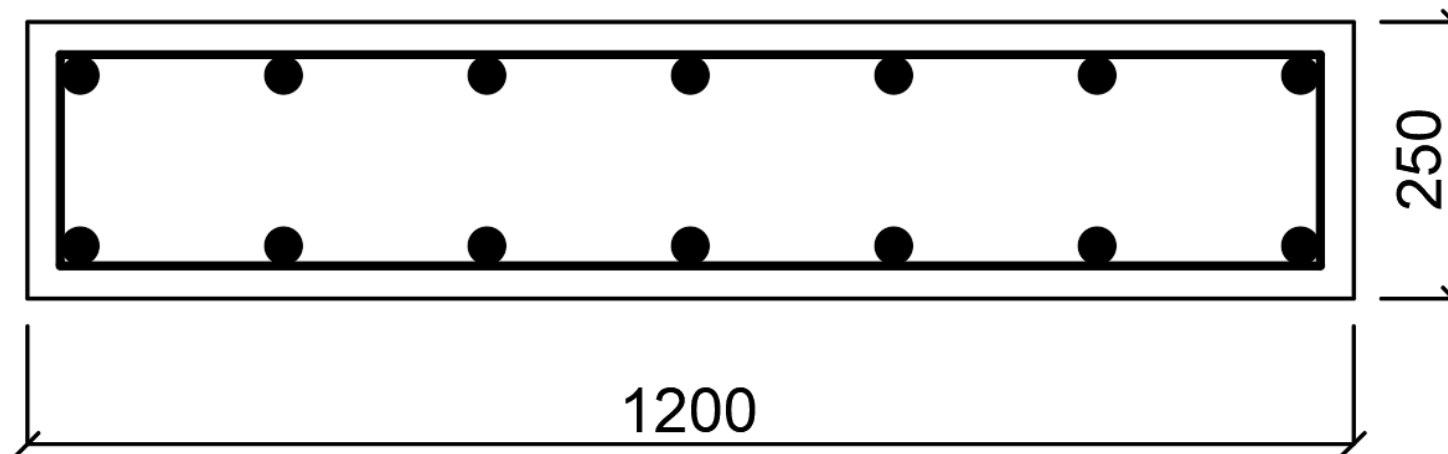
$$M_{rd} = \dots$$

Don't forget to also check the detailing rules!

Design of reinforcement

For planar members (such as slabs), we usually calculate the moment and reinforcement per 1 m, but **in the case of staircase** (both landing and flight) we **use the real width** – i.e., we design it like a flat beam:

$$M_{Ed} \text{ [kNm]} \rightarrow n \times \varnothing \rightarrow A_s \text{ [mm}^2\text{]} \rightarrow M_{Rd}$$



Sketch of reinforcement

Sketch of reinforcement

Sketch the reinforcement of **both flights**.

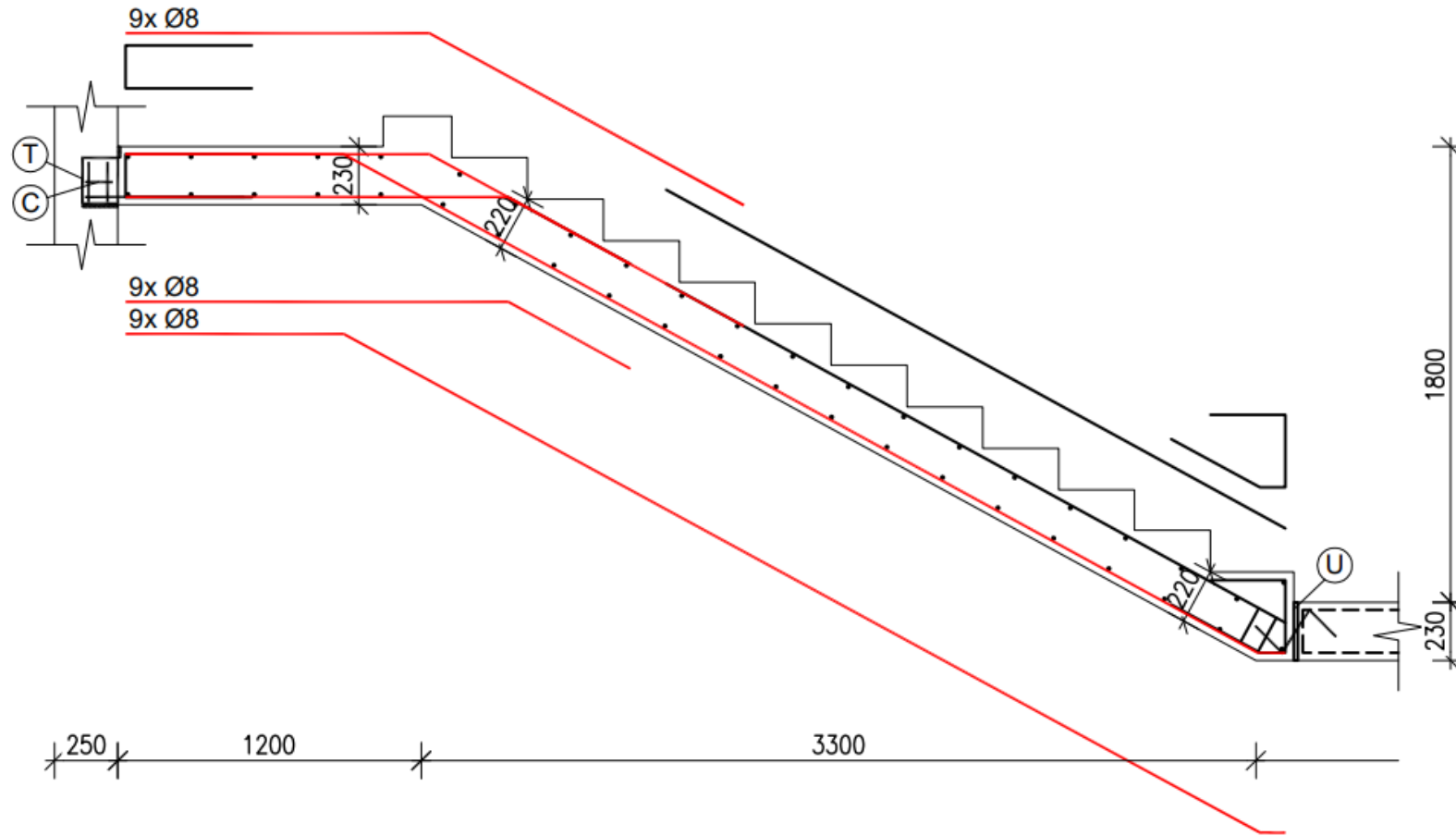
Main reinforcement:

- draw the shapes **in red colour**.
- write the **number and diameter of bars** according to design.

Secondary reinforcement:

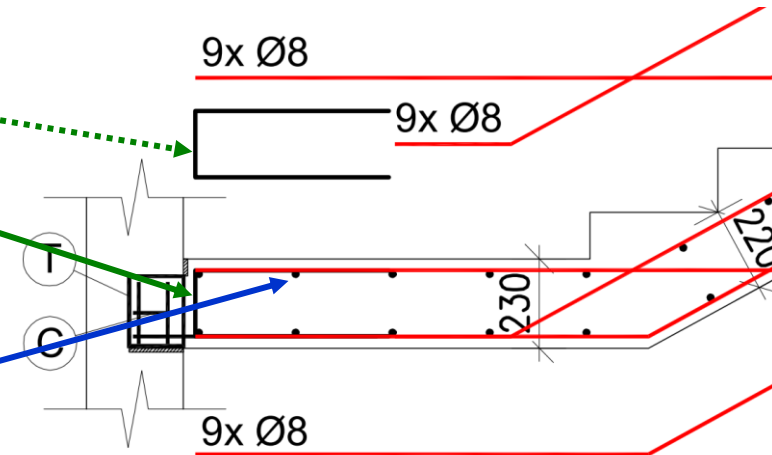
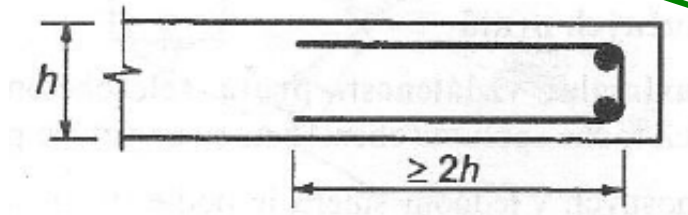
- draw the shapes in **black colour**,
- consists of:
 - edge reinforcement,
 - transverse reinforcement,
 - secondary reinforcement of the upper surface,
 - end stirrups.

Primary reinforcement



Secondary reinforcement

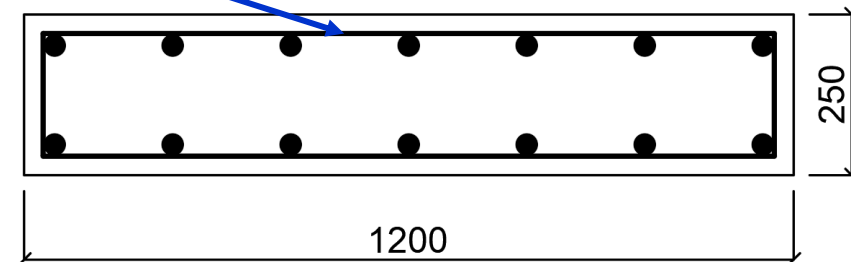
Edge reinforcement:



Transverse reinforcement:

$$a_{s, tr} \geq 0.25 a_{s, main}$$

$$s_{tr} \leq \min(3h; 400 \text{ mm})$$

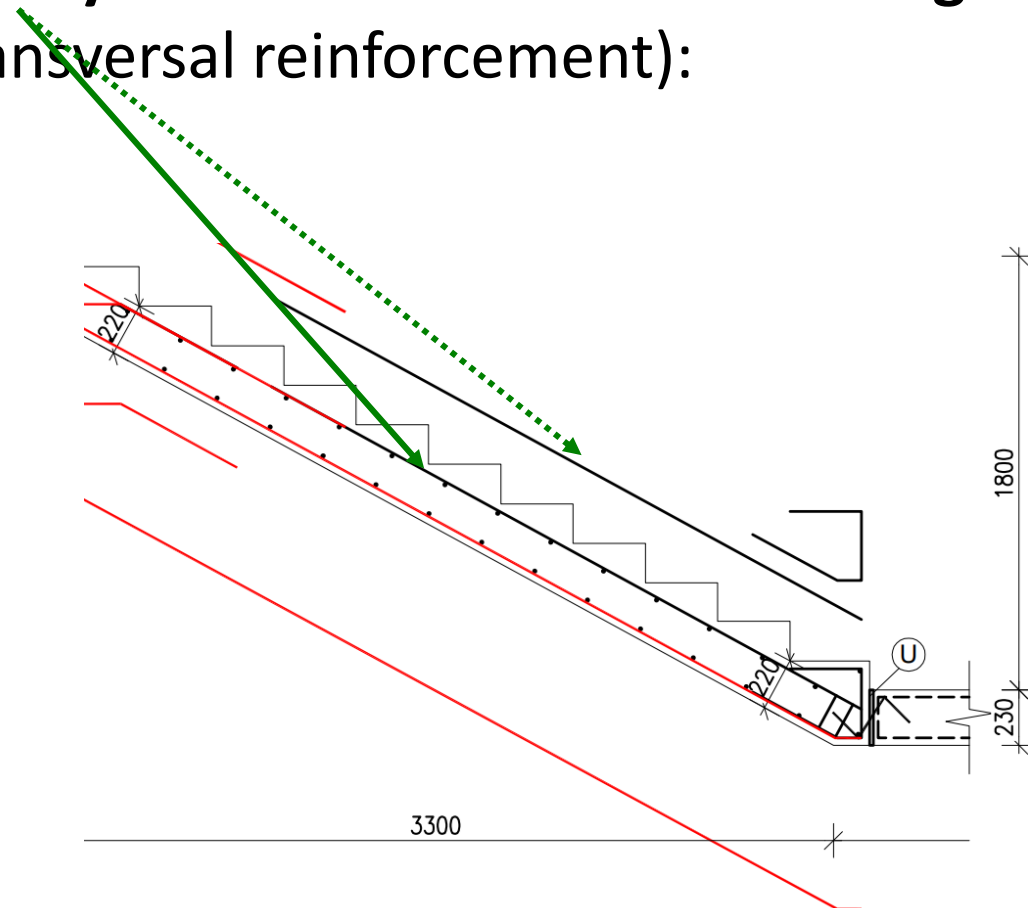


Secondary reinforcement

In the **places where no main reinforcement was designed** (e.g., upper reinforcement in the flight), **secondary reinforcement must be designed** using detailing rules (same rules as for transversal reinforcement):

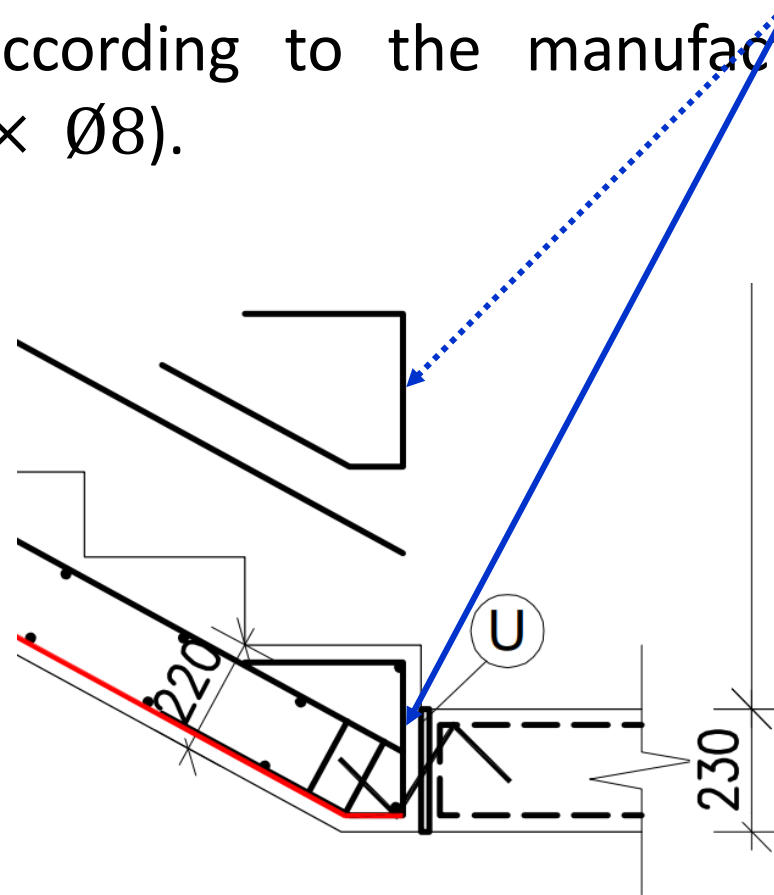
$$a_{s,tr} \geq 0.25a_{s,\text{main}}$$

$$s_{tr} \leq \min(3h; 400 \text{ mm})$$

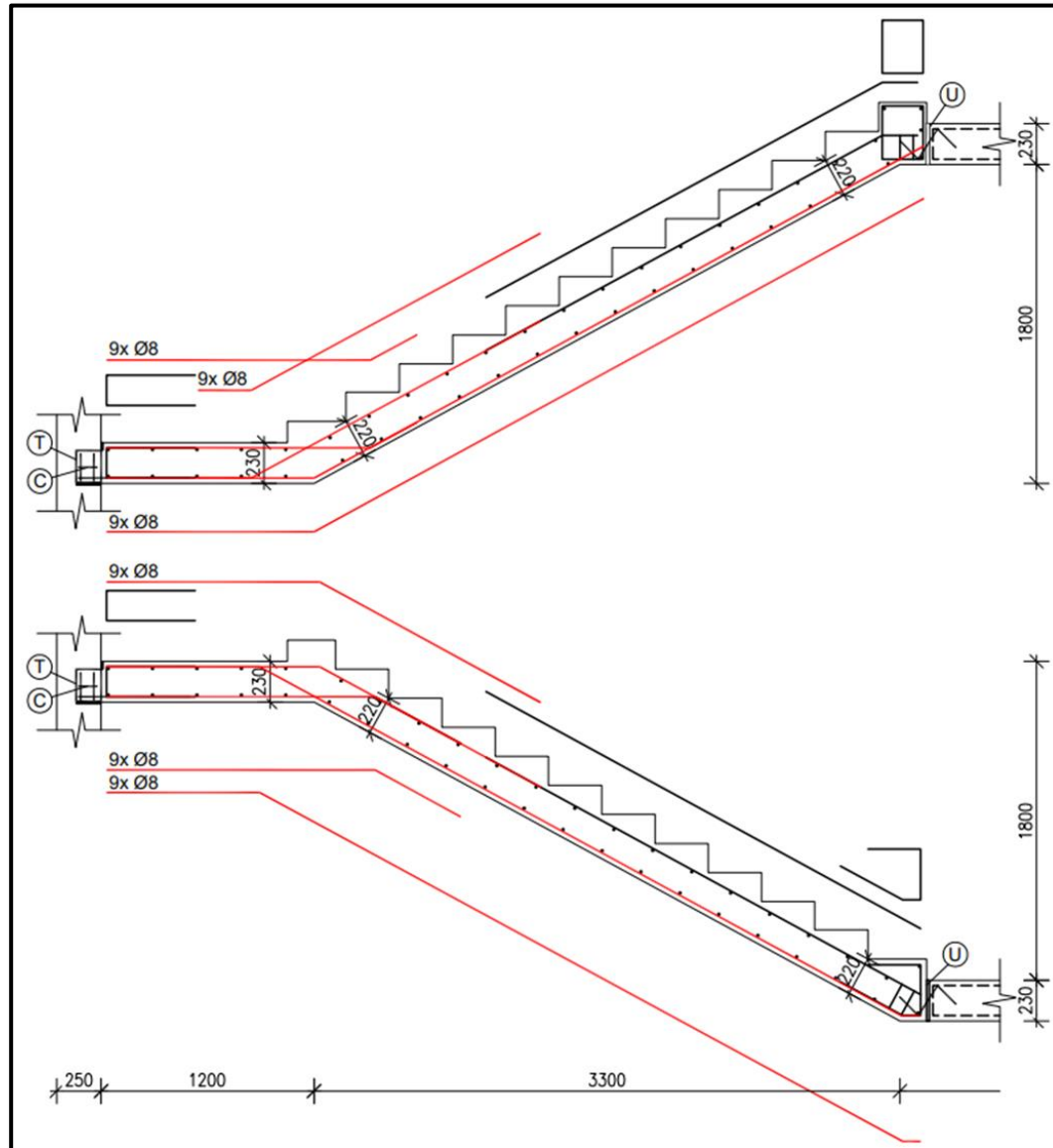


Secondary reinforcement

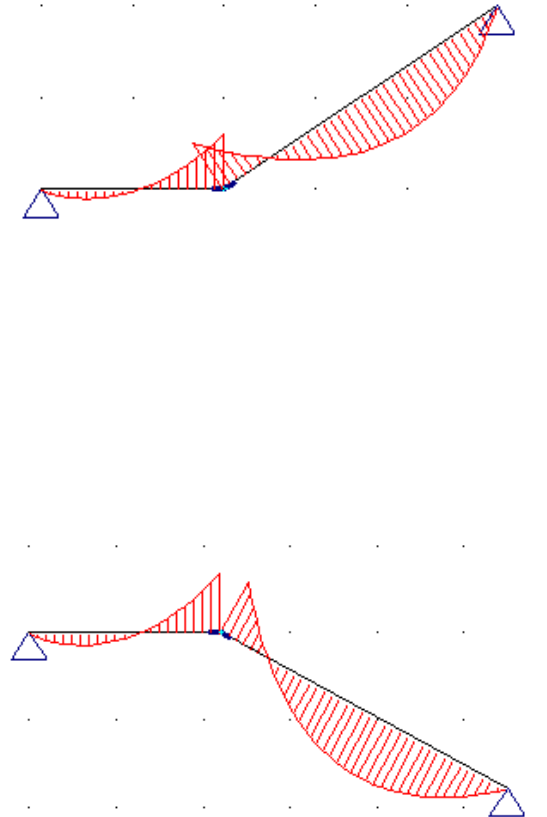
At the end of each reinforced concrete members, **end stirrups** must be used. End stirrups are designed according to the manufacturer of the sound insulation elements (usually $2 \times \text{Ø}8$).



Sketch of reinforcement



Corresponding
bending moments



thank you for your attention

Recognitions

I thank **Assoc. Prof. Petr Bílý** for his original seminar presentation and other supporting materials from which this presentation was created.