

2nd TASK: TWO-WAY SLAB SUPPORTED ON 4 SIDES

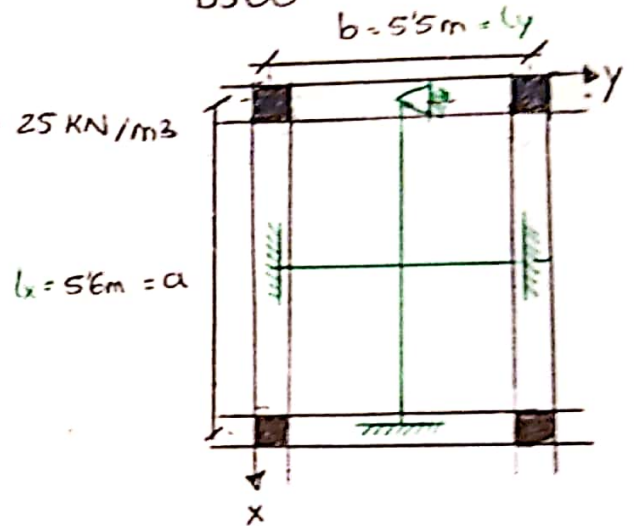
- DATA -

Scheme B
Member P2
 $b = 5.5\text{ m}$
 $a = 5.6\text{ m}$
 $h_s = 180\text{ mm}$

Loads: $(g-g_c)_{\text{floor},k} = 1.1\text{ kN/m}^2$
 $q_{\text{floor},k} = 2.9\text{ kN/m}^2$

Material: C 25/30
B500

Weight of the concrete = 25 kN/m^3



- LOADS -

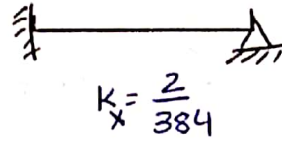
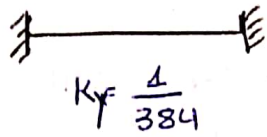
PERMANENT	K-VALUE [KN/m ²]	Y	d-value [KN/m ²]
self-weight $25 \frac{\text{KN}}{\text{m}^3} \cdot 0.18\text{ m}$	4.5	1.35	6.075
$(g-g_c)_{\text{floor},k}$	1.1	1.35	1.485
VARIABLE $q_{\text{floor},k}$	2.9	1.5	4.35
	<u>8.5 KN/m²</u>		<u>11.91 KN/m²</u>

- LINEAR ANALYSIS -

$$f_{d,x} = \frac{f_d \cdot \frac{K_y}{K_x} \cdot \left(\frac{L_y}{L_x}\right)^4}{1 + \frac{K_y}{K_x} \cdot \left(\frac{L_y}{L_x}\right)^4}$$

$$f_{d,y} = f_d - f_{d,x}$$

where K :



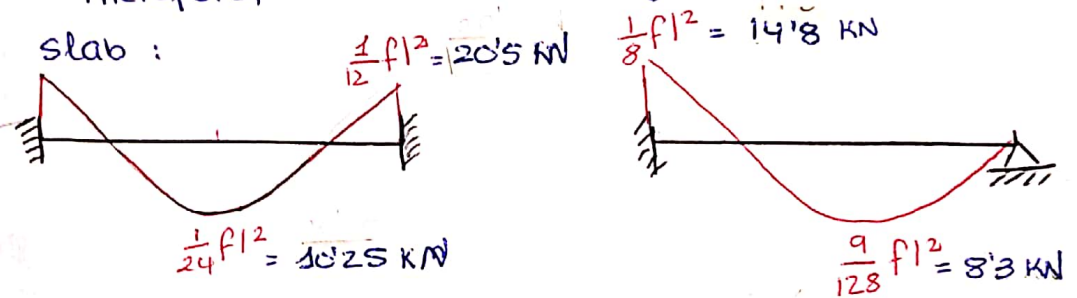
$$So: f_{dx} = 11'91 \cdot \frac{1/384}{2/384} \cdot \left(\frac{5'5}{5'6} \right)^4$$

$$= 3'78 \text{ KN/m}^2$$

$$f_{dy} = 11'91 - 3'78 = 8'13 \text{ KN}$$

Therefore, the linear bending moments in the

slab :



$$\bullet \frac{1}{12} \cdot f_{dy} \cdot l_y^2 = \frac{1}{12} \cdot 8'13 \cdot 5'5^2$$

$$= 20'5 \text{ KN}$$

$$\bullet \frac{1}{24} \cdot 8'13 \cdot 5'5^2 = 10'25 \text{ KN}$$

$$\bullet \frac{1}{8} f_{dx} \cdot l_x^2 = \frac{1}{8} \cdot 3'78 \cdot 5'6^2$$

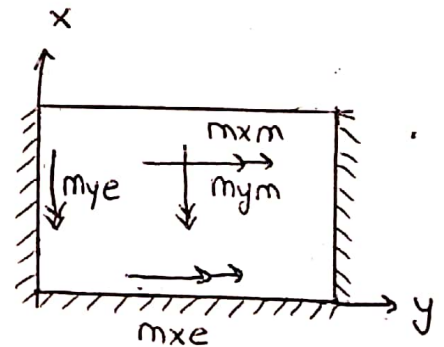
$$= 14'8 \text{ KN}$$

$$\bullet \frac{9}{128} \cdot 3'78 \cdot 5'6^2 = 8'3 \text{ KN}$$

- PLASTIC ANALYSIS -

$$\bullet \frac{l_y}{l_x} \rightarrow \beta$$

$$\frac{5'6}{5'5} = 1'02$$



So, interpolating, I obtained from the table:

$$\beta_{xe} = -0'041$$

$$\beta_{xm} = 0'0312$$

$$\beta_{ye} = -0'0296$$

$$\beta_{ym} = 0'0224$$

l_x is the shorter span, in this case:

$$l_x = 5'5 \text{ m}$$

$$l_y = 5'6 \text{ m}$$

The bending moments:

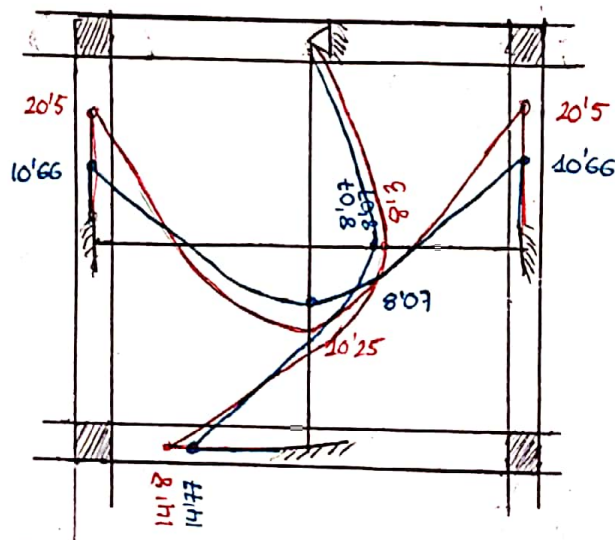
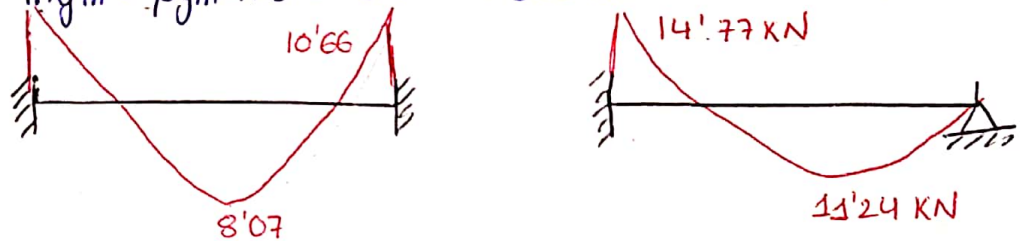
$$M_0 = f_d \cdot Lx^2 = 11'91 \cdot 5'5^2 = 360'27 \text{ KN}$$

$$M_{xe} = \beta_{xe} \cdot M_0 = -0'041 \cdot 360'27 = -14'77 \text{ KN}$$

$$M_{xm} = \beta_{xm} \cdot M_0 = 0'0312 \cdot 360'27 = 11'24 \text{ KN}$$

$$M_{ye} = \beta_{ye} \cdot M_0 = -0'0296 \cdot 360'27 = -10'66 \text{ KN}$$

$$M_{ym} = \beta_{ym} \cdot M_0 = 0'0224 \cdot 360'27 = 8'07 \text{ KN}$$



— Linear Analysis
— Plastic Analysis

- CHECK OF h_s -

$$a_{s, reqd} = \frac{M_{ed, max}}{0'9 \cdot d \cdot f_{yd}} \quad \text{where } d = h_s - \frac{\phi}{2} - c$$

assuming rebars $\phi 10$ mm and a cover depth $c = 20$ mm (from frame structure)

$$d = 180 - \frac{10}{2} - 20 = 155 \text{ mm}$$

$$\rightarrow a_{s, reqd} = \frac{14'77}{0'9 \cdot 0'155 \cdot 434'78} = 243'5 \text{ mm}^2$$

$M_{ed, max}$ from the plastic analysis:

$$M_{ed, max} = 14'77 \text{ KN}$$

for S500

$$f_{yd} = \frac{500}{1'15} = 434'78 \text{ MPa}$$

for C25/30

$$f_{cd} = \frac{25}{1'5} = 16'67 \text{ MPa}$$

So, the depth of the compressed zone:

$$x = \frac{1'2 \cdot a_{s, reqd} \cdot f_{yd}}{0'8 \cdot b \cdot f_{cd}} \quad \text{where } b = 1000 \text{ mm for slabs}$$

$$x = \frac{1'2 \cdot 243'5 \cdot 434'78}{0'8 \cdot 1000 \cdot 16'67} = 9'52 \text{ mm}$$

$$1. a_{s, \text{reqd}} \geq a_{s, \text{min}}$$

$$a_{s, \text{min}} = \max \left(0'26 \frac{f_{ctm}}{f_{yk}} \cdot b_s \cdot h_s ; 0'0013 \cdot b_s \cdot h_s \right)$$

$$a_{s, \text{min}} = \max \left(0'26 \frac{2'6}{500} \cdot 1000 \cdot 180 ; 0'0013 \cdot 1000 \cdot 180 \right)$$

$$a_{s, \text{min}} = \max (243'36 ; 234)$$

$$a_{s, \text{min}} = 243'36 \text{ mm}^2$$

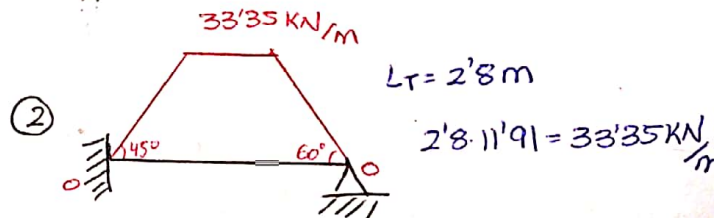
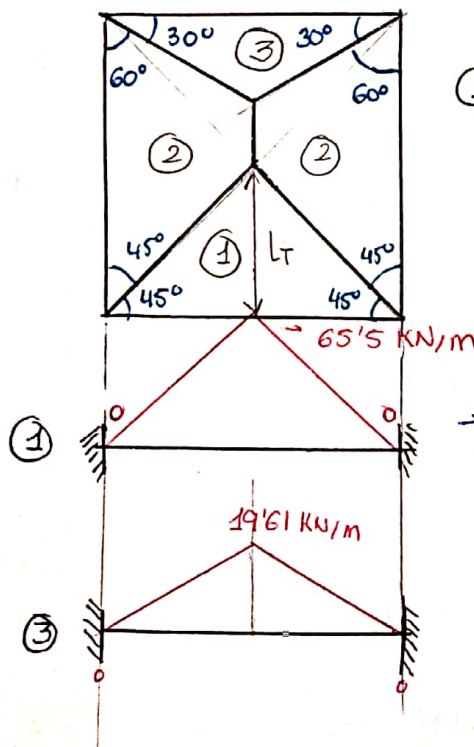
$$243'5 \text{ mm}^2 = a_{s, \text{reqd}} \geq a_{s, \text{min}} = 243'36 \text{ mm}^2 \checkmark$$

$$2. \xi = \frac{x}{d} \leq 0'25$$

$$\xi = \frac{9'52}{155} = 0'06 \leq 0'25 \checkmark$$

Therefore h_s is checked

- LOAD DIAGRAM -



$$L_T = 2'75 \text{ m}$$

$$\rightarrow 2 \cdot L_T \cdot f_d =$$

$$2 \cdot 2'75 \cdot 11'91 = 65'5 \text{ kN/m}$$

$$L_T = 1'65 \text{ m}$$

$$1'67 \cdot 11'91 = 19'61 \text{ kN}$$

$f_{ctm} = 2'6 \text{ MPa}$ for
C25/30