Prestressed Concrete

Part 4

(Losses of prestress)

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Prestressing force

- Prestressing force varies along the length of the tendon and also over the time.
- Prestressing force significantly influences the behaviour of the structure.
- Necessary to known the value of prestressing force in every point of the tendon.
- We derive it from the stress of reinforcement before anchoring in the section at the stressed end.

stress before anchoring of reinforcement  stress introduced by the jack
Mean value of prestressing force at the end of member

mean value of prestressing stress at the end of member
Mean values of prestressing force and stress during time

<table>
<thead>
<tr>
<th>time</th>
<th>scheme</th>
<th>force</th>
<th>stress</th>
<th>limitation of stress</th>
</tr>
</thead>
<tbody>
<tr>
<td>stretching</td>
<td><img src="image1" alt="Diagram" /></td>
<td>$P_{\text{max}}$</td>
<td>$\sigma_{p,\text{max}}$</td>
<td>$\sigma_{p,\text{max}} \leq \min(0,8 f_{pk}; 0,9 f_{p0,1k})$</td>
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<tr>
<td>$t = 0$</td>
<td></td>
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<tr>
<td>after anchoring</td>
<td><img src="image2" alt="Diagram" /></td>
<td>$P_{m0}(x)$</td>
<td>$\sigma_{pm0}(x)$</td>
<td>$\sigma_{pm0}(x) \leq \min(0,75 f_{pk}; 0,85 f_{p0,1k})$</td>
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<tr>
<td>$t = t_0$</td>
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<tr>
<td>during service life</td>
<td><img src="image3" alt="Diagram" /></td>
<td>$P_{mt}(x)$</td>
<td>$\sigma_{pmt}(x)$</td>
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<tr>
<td>$t$</td>
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<tr>
<td>after service life</td>
<td><img src="image4" alt="Diagram" /></td>
<td>$P_{m\infty}(x)$</td>
<td>$\sigma_{pmt}(x)$</td>
<td>$\sigma_{pm\infty}(x) \leq 0,75 f_{pk}$</td>
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<td>$t = \infty$</td>
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</table>

*) mean values acting in tendons at time $t$ and distance $x$
Scheme of considering states of prestressed members

<table>
<thead>
<tr>
<th>State</th>
<th>Scheme</th>
<th>Prastressing force</th>
<th>Criteria - check</th>
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<tr>
<td>Stadium of prestressing</td>
<td><img src="image1" alt="Diagram" /></td>
<td>$P_{ki} = r_i P_{m0}$</td>
<td>stress in concrete $\sigma_c$ and in prestressing steel $\sigma_p$</td>
</tr>
<tr>
<td>SLS</td>
<td><img src="image2" alt="Diagram" /></td>
<td></td>
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</tr>
<tr>
<td>Stadium of service</td>
<td><img src="image3" alt="Diagram" /></td>
<td>$P_{ki} = r_i P_{m0}$</td>
<td>stress in concrete $\sigma_c$ and in prestressing steel $\sigma_p$ width of crack $w_k$ deflection $f_d$</td>
</tr>
<tr>
<td>SLS</td>
<td><img src="image4" alt="Diagram" /></td>
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<tr>
<td>ULS</td>
<td><img src="image5" alt="Diagram" /></td>
<td>$P_{\infty} = \gamma_p P_{m0}$</td>
<td>ultime resistance $M_{Rd}$ $N_{Rd}$ $V_{Rd}$</td>
</tr>
<tr>
<td></td>
<td><img src="image6" alt="Diagram" /></td>
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<td></td>
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</tbody>
</table>

a) to e) distribution of stresses in cross section; $r_i$ - allowance for possible variation in prestress
• Maximum stress in tendon before anchoring (at the active end during prestressing, acts for a short time period - EN 1992-1-1):

\[ \sigma_{p,\text{max}} = \min(0.8 f_{pk} ; 0.9 f_{p0,1k} ) \]

- \( f_{pk} \) characteristic tensile strength of prestressing reinforcement
- \( f_{p0,1k} \) characteristic 0.1% proof-stress of prestressing reinforcement

• Changes occur at the time of prestressing, during anchoring and after anchoring (short and long term losses) along the length of the tendon
Short-term (immediate) losses due to:

- friction between tendon and wall of duct,
- anchorage set loss (friction anchorage),
- immediate elastic strain in the concrete during stressing,
- sequential prestressing (phases of prestress.),
- relaxation of prestressing reinforcement (before transfer),
- deformation of end abutments of stressing bed,
- differences in temperature of prestressing reinforcement end stressing bed,
- bearing pressure on concrete – circumferential tendons with small radius of curvature
Long-term (service life) losses caused by:

• relaxation of prestressing reinforcement (after transfer),
• shrinkage of concrete,
• creep of concrete,
• creep of concrete due to many repeated cyclic load,
• immediate elastic strain in concrete due to variable load
Simplifying assumptions for calculation of losses:

• Concrete and prestressing steel for short term effects of load – assume ideally elastic matters. Steel stress reaches the highest value at the instant of stressing, under low stresses behaves linearly. Instantaneous inelastic concrete strain is very small.

• Perfect bond between concrete and steel only for bonded prestressing steel (the strain of adjoining steel fibre and concrete fibre are the same).

• Prestressing force acts in the centre of gravity of the area of prestressing reinforcement.

• Short-term losses are calculated separately.
Transformed (idealized) cross section

Fictitious substitute cross section consisting of:

a) concrete compressed part of the cross section,
b)- $\alpha_p$ multiple of sectional area of prestressing reinforcement,
c)- $\alpha_e$ multiple of sectional area of reinforcement,

where $\alpha_p = \frac{E_p}{E_{cm}}$; $\alpha_e = \frac{E_s}{E_{cm}}$

Calculate:

$A_i = A_c + \alpha_p A_p + \alpha_e A_s$ ; $l_i$ ; $W_i$ etc.
Idealized cross section – acts full concrete cross section

Idealized cross section – acts part of concrete cross section
Loss of prestressing due to friction

- **Pre-tensioned prestressed concrete** – rarely, (only at elevating prestressing steel)
• Post-tensioned prestressed concrete—especially, during the stressing occurs friction between the tendon and wall of the tendon duct
• The loss consists of two components:
  - curvature frictional loss (curved part of tendon)
  - wobble frictional loss
Intentional change of direction – curvature frictional loss

\[ t = \mu r \] ; \( \mu \) is the friction coefficient;

\[ r \] the force per unit length perpendicular to tendon

radial force \( R \) is in equilibrium with forces \( P \) \( \Rightarrow \) \( R \approx P \, d\alpha \)

\[ dP = -\mu \, P \, d\alpha \]
Unintentional change of direction – wobble frictional loss

Tendon duct fixed by spacers – between them the duct deforms due its self-weight and to occasional unevenness, thus forming an unintentional wobbles

Unintentional angular change over the length $dl$ is expressed as $k dl$; $k$ – empirically determined unintended angular change per unit length of the tendon

$$dP = -\mu P d\alpha - \mu P_k dl$$
The total change in prestressing force between the points A and B

\[ \int_{P_A}^{P_B} \frac{dP}{P} = -\mu \int_0^\alpha d\alpha - \mu k \int_0^l dl = -\mu \left( \int_0^\alpha d\alpha - k \int_0^l dl \right) \]

- \(P_A\) is the prestressing force in point A,
- \(P_B\) is the prestressing force in point B,
- \(\alpha\) is the total intended angular change along the length A and B,
- \(L\) is the total length of the tendon between the points A and B

Note: L can be substitute by perpendicular projection of the tendon into the horizontal axis \(l\)

From the solution we receive

\[ P_B = P_A e^{-\mu(\alpha-kl)} \]

From the difference of forces we obtain loss and then the loss of prestressing stress related to the stress at stressed end \(\sigma_{p0,0}\)

\[ \Delta\sigma_{p\mu}(l) = -\sigma_{p0,0} \left( 1 - e^{-\mu(\alpha+kl)} \right) \]
**Coefficients of friction $\mu$ of post-tensioned internal tendons and external unbonded tendons**

<table>
<thead>
<tr>
<th></th>
<th>Internal tendons ¹)</th>
<th>External unbonded tendons</th>
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<th></th>
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<tbody>
<tr>
<td></td>
<td>Steel duct/</td>
<td>HDPE duct/</td>
<td>Steel duct/</td>
<td>HDPE duct/</td>
</tr>
<tr>
<td></td>
<td>non lubricated</td>
<td>non lubricated</td>
<td>lubricated</td>
<td>lubricated</td>
</tr>
<tr>
<td>Cold drawn wire</td>
<td>0,17</td>
<td>0,25</td>
<td>0,14</td>
<td>0,18</td>
</tr>
<tr>
<td>Strand</td>
<td>0,19</td>
<td>0,24</td>
<td>0,12</td>
<td>0,16</td>
</tr>
<tr>
<td>Deformed bar</td>
<td>0,65</td>
<td>-</td>
<td>-</td>
<td>-</td>
</tr>
<tr>
<td>Smooth round bar</td>
<td>0,33</td>
<td>-</td>
<td>-</td>
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</tr>
</tbody>
</table>

¹) for tendons which fill about half of the duct

**Note:** HPDE - High density polyethylene

**Values $k$ for unintended regular displacements for internal tendons** will generally be in the range $0,005 < k < 0,01$ per meter
\[ \sigma_p \quad [\text{MPa}] \]

friction

\[ \sigma_{p0} \quad \Delta \sigma_p \]

- tendon stressed from A

\[ \sigma_{p0,A} \]

0(A)

\[ x[\text{m}] \]
Anchorage set loss

- Drawn-in the wedge and the strand in the anchor head result in the reduction of stress in the prestressing reinforcement – anchorage set loss

- **Anchorage set loss - friction not taken in account**

  - set $w$ decreases elongation $\Delta l$ of the stressed tendon with the length $l \Rightarrow$ anchorage set loss

\[ \Delta \sigma_{pw} = - \frac{wE_p}{l} \]
• Anchorage set loss when tendon is stressed from one end only – friction take into account

• Post-tensioned prestressed concrete

• When the tendon is anchored, stress $\sigma_{p0,A}$ on the stressed end decreases due to movement of the tendon to the non-stressed anchor $\Rightarrow$ arises the friction in the opposite direction

\[
\Delta \sigma_{pw} = \sigma_{pa,A} e^{\mu(a_x+kx_w)} - \sigma_{p0,A} e^{-\mu(a_x+kx_w)}
\]
$\Delta \sigma_{pw} = -184.42$ m

$x_w = 15.834 \, m$

$\alpha_w = 9.881^\circ$

- red: tendon stressed from A
- dashed: tendon stressed from A only and then anchored at A
• **Anchorage set loss when tendon is stressed from both ends**

• Post-tensioned prestressed concrete

• Let us suppose the following procedure of stressing:
  - stressing of the tendon from end A
  - stressing of the tendon from end E
  - anchoring the tendon at end A
  - anchoring the tendon at end E

• Decrease of the stress due to friction
The advantage depends on the size of anchorage set during anchoring.
Loss of prestressing due to immediate elastic strain in concrete

- **Load from prestressing** – one of many possible loads
- This load changes the stress state of the tendon and results in losses in prestressing
- **The pre-tensioned strand** is at the moment of the introduction of prestressing already the part of the prestressed element and resists the load introduced by itself ⇒ the loss of pressing due to immediate strain in concrete takes place
- **The pre-tensioned strand in duct** connects at the moment of the introduction of prestressing with the concrete only at the anchorages ⇒ the loss of pressing due to immediate strain in concrete at the moment of the introduction of prestressing = 0 (the loss is equilibrated by re-stretching of strand)
Pre-tensioned prestressed concrete – loss due to immediate elastic strain in concrete

- **Transfer of prestressing** – by releasing the pre-tensioned prestressing reinforcement from anchorage abutments, the reinforcement acts with the concrete as a part of element → any load results in an immediate deformation of the element and thus deformation of the tendon
(a) Distribution of internal forces before release of strands by cutting

\[ \Delta N_c = P - \Delta P \]

(b) Distribution of internal forces after transfer of prestressing
\[ \Delta N_c = P - \Delta P \quad \Delta \varepsilon_c = \frac{\Delta N_c}{A_c E_c}; \quad \Delta \varepsilon_p = \frac{P - \Delta N_c}{A_p E_p} \]

\[
\frac{\Delta N_c}{A_c E_c} = \frac{P - \Delta N_c}{A_p E_p} \Rightarrow \Delta N_c = \frac{P A_c E_c}{A_c E_c + A_p E_p} = \frac{P}{1 + \frac{A_p E_p}{A_c E_c}}
\]
Post-tensioned prestressed concrete – loss due to immediate elastic strain in concrete

The tendon is not a part of prestressed element at the moment of stressing and does not resist the load introduced by itself. The tendon is re-stressed to the original value of the prestressing force ⇒ the loss of prestressing due to immediate elastic strain at the moment of the introduction of prestressing in the concrete is zero.
Loss of prestressing due to sequential stressing

Post-tensioned prestressed concrete – results of immediate elastic strain in the concrete and already anchored reinforcement during successive stressing of other tendons. Tendons stressed and anchored simultaneously ⇒ loss = 0

\[ A_c; A_p, \text{ stressing force } P_0 \]

1. tendon: \( A_p/m \)

\[ P=P_0/m \cdot \Delta_1 l \] deformation eliminated by the by piston stroke of jack ⇒ \( \Delta_1 P = 0 \)

2. tendon: \( \Delta_2 P = 0; \Delta_1 P \neq 0 \)

\[ P_1 = P - \Delta_2 P \]

j. tendon: \( P_1 = P - \Delta_2 P - \ldots - \Delta_j P \)

\[ \Delta_j \varepsilon_c = -\frac{\Delta_j P}{A_p} \]; \( \Delta_j P = \frac{P A_p E_p}{m A_c E_c + (j-1) A_p E_p} \)
When the j-th tendon is being stressed, loss $\Delta_j P \neq 0$ takes place in all (j-1)tendons and results in their shortening

$$\Delta_j \varepsilon_c = \frac{-\Delta_j P}{A_p E_p m}$$

The total increment of the force acting in the concrete is $P - (j-1)\Delta_j P$ and leads to the shortening of the concrete

$$\Delta_j \varepsilon_c = \frac{-\left(P - (j-1)\Delta_j P\right)}{A_c E_c}$$

The loss of force in each of the (j-1) tendons during stressing of the j-th tendon is

$$\Delta_j P = \frac{PA_p E_p}{mA_c E_c + \left(j - 1\right)A_p E_p}$$
This loss due to sequential stressing may be assumed as a mean loss in each tendon as follows:

$$\Delta P_{el} = A_p \cdot E_p \cdot \sum \left[ \frac{j \cdot \Delta \sigma_c(t)}{E_{cm}(t)} \right]$$

where

- $\Delta \sigma_c(t)$ is the variation of stress at the centre of gravity of the tendons applied at time $t$
- $j$ is a coefficient equal to
  - $j = (n-1)/2n$ where $n$ is the number of identical tendons successively prestressed; as an approximation $j$ may be taken as $1/2$
  - $j = 1$ for the variations due to permanent actions applied after prestressing.
Loss of prestressing due to elastic strain in concrete resulting from external load

- **Losses in service life** – takes place after anchoring, or after transfer.
- The action of **external load** (superimposed dead load, variable load, etc.) is similar to the action of pre-tensioned prestressed strand during the introduction of prestressing – the prestressing reinforcement is a part of the element ⇒ the loss of prestressing due to strain in concrete takes place.
Loss of prestressing due to relaxation of prestressing reinforcement

Time dependent properties of prestressing steel

Real stress-strain diagram of prestressing wires/strands
In EN 1992-1-1, three classes of relaxation are defined:

Class 1: wire or strand - ordinary relaxation
Class 2: wire or strand - low relaxation
Class 3: hot rolled and processed bars

\[
\frac{\Delta \sigma_{pr}}{\sigma_{pi}} = 5.39 \quad \rho_{1000} \cdot e^{6.7 \mu \left( \frac{t}{1000} \right)^{0.75 (1-\mu)}} 10^{-5}
\]

\[
\frac{\Delta \sigma_{pr}}{\sigma_{pi}} = 0.66 \quad \rho_{1000} \cdot e^{9.1 \mu \left( \frac{t}{1000} \right)^{0.75 (1-\mu)}} 10^{-5}
\]

\[
\frac{\Delta \sigma_{pr}}{\sigma_{pi}} = 1.98 \quad \rho_{1000} \cdot e^{8 \mu \left( \frac{t}{1000} \right)^{0.75 (1-\mu)}} 10^{-5}
\]

\(\Delta \sigma_{pr}\) is absolute value of the relaxation losses of the prestress
\(\sigma_{pi}\) for post-tensioning \(\sigma_{pi}\) is the absolute value of the initial prestress
\(\sigma_{pi} = \sigma_{pm0}\); for pre-tensioning \(\sigma_{pi}\) is the maximum tensile stress applied to the tendon minus the immediate losses occurred during the stressing process
\(t\) the time after tensioning (in hours)
\(\mu = \sigma_{pi} / f_{pk}\), where \(f_{pk}\) is the characteristic value of the tensile strength of the prestressing steel
\(\rho_{1000}\) the value of relaxation loss (in %), at 1000 hours after tensioning and at a mean temperature of 20°C.
Loss of prestressing due to relaxation

- Applies to both production and service stages
- The size of relaxation depends on the
  - class, indicating the relaxation behaviour
  - level of introduced prestressing
  - time

Correction of relaxation through keeping constant stress during stressing
Loss of prestressing due to deformation of end abutments of stressing bed

• Pre-tensioned prestressed concrete – abutments deform due to sequential stressing

• Assume $m$ identical and identically stressed strands results in total force $P$. If $P$ is introduced as a stroke, the distance $l_p$ between anchorage abutments would shorten by value $\Delta l_p$. The strain in tendons is $\varepsilon_p = \Delta l_p / l_p$; in one tendon $\varepsilon_{p1} = \varepsilon_p / m$, the loss in in all $j-1$ anchored strands

$$\Delta \sigma_{pA1} = -E_p \varepsilon_{p1} = -E_p \frac{\Delta l_p}{l_p m}$$

• Average loss in each strand after sequential stressing

$$\Delta \sigma_{pA} = \frac{1}{m} \sum_{i=1}^{m} \left( -E_p \left( \frac{m-1}{m} \right) \frac{\Delta l_p}{l_p} \right) = -E_p \frac{m-1}{2m} \frac{\Delta l_p}{l_p}$$
Loss due to differences in the temperature of prestressing reinforcement and stressing bed

- Pre-tensioned prestressed concrete – eg. by steam curing of concrete
- Assume the distance between abutments $l_A$, the length of the prestressing reinforcement $l_p$ with the difference of temperature $\Delta T_p$. Due to change in temperature the distance between anchorage abutments will be $\Delta l_p = \alpha_p \Delta T_p/l_p$, where $\alpha_p$ is the coefficient of thermal expansion of the prestressing reinforcement.
- The difference strain in tendons $\Delta \varepsilon_{pT} = \Delta l_p/l_A$; the loss will be

$$\Delta \sigma_{pT} = -E_p \varepsilon_p = -E_p \frac{\alpha_p \Delta T_p l_p}{l_A}$$
Draw-in loss of prestressing

- **Wire wound structure** – with small radius of curvature
- **Assume a differential element of the wound tendon**

\[ \Delta l = (r - \Delta r)d\alpha - rd\alpha = -\Delta rd\alpha \]

\[ \Delta \sigma_{po} = E_p \frac{-\Delta rd\alpha}{rd\alpha} = -E_p \frac{\Delta r}{r} \]
• **Maximum stress in tendon after anchoring**
  (stage of transfer the prestressing force to concrete):

\[
\sigma_{p,\text{max}} = \min(0.75 f_{pk}; 0.85 f_{p0,1k})
\]

- \( f_{pk} \) characteristic tensile strength of prestressing reinforcement
- \( f_{p0,1k} \) characteristic 0.1% proof-stress of prestressing reinforcement
Long term main losses of prestressing due to shrinkage and creep of concrete and relaxation of prestressing steel

- Calculation is generally complex
- Creep – long term loads

\[
\varepsilon_{cc} = \frac{\sigma_{cp}}{E_c(t)} \varphi(t_0, t)
\]

Stress state due to long-term loads \((g + \varphi_2 q + P)\) affecting the creep of concrete
Derivation of basic formula for shrinkage

\[ \varepsilon_{c,cs} = \left( \frac{\Delta N_{p,cs}}{A_c} + \frac{\Delta N_{p,cs} z_{cp}^2}{I_c} \right) \frac{1 + 0.8 \varphi}{E_{cm}} \]
Derivation of basic formula for shrinkage

\[ \varepsilon_{cs} = \frac{\Delta N_{p,cs}}{A_p E_p} + \frac{\Delta N_{p,cs}}{A_c E_{cm}} \left( 1 + \frac{A_c}{I_c} z_{pc}^2 \right) (1 + 0,8 \varphi) \]

\[ \Delta N_{p,cs} = \frac{\varepsilon_{cs} A_p E_p}{1 + \frac{A_p E_p}{A_c E_{cm}} \left[ \left( 1 + \frac{A_c}{I_c} z_{pc}^2 \right) (1 + 0,8 \varphi) \right]} \]

\[ \Delta \sigma_{p,cs} = \frac{\varepsilon_{cs} A_p E_p}{1 + \sigma_e \frac{A_p}{A_c} \left( 1 + \frac{A_c}{I_c} z_{pc}^2 \right) (1 + 0,8 \varphi)} \]

\[ \Delta \sigma_{p,cs} = \frac{\varepsilon_{cs} A_p E_p}{A} \]
\[
\Delta P_{c+s+r} = A_p \Delta \sigma_{p,c+s+r} = A_p \left( \frac{\varepsilon_{cs} E_p + 0.8 \Delta \sigma_{pr} + \frac{E_p}{E_{cm}} \varphi(t,t_0) \sigma_c \cdot Q_P}{1 + \frac{E_p}{E_{cm}} \frac{A_p}{A_c} \left(1 + \frac{A_c}{I_c} z_{cp}^2 \right) [1 + 0.8 \varphi(t,t_0)]} \right)
\]

\(\Delta \sigma_{p,c+s+r}\) is the absolute value of the variation of stress in the tendons due to creep, shrinkage and relaxation at location \(x\), at time \(t\)

\(\varepsilon_{cs}\) is the estimated shrinkage strain in absolute value

\(E_p\) is the modulus of elasticity for the prestressing steel

\(E_{cm}\) is the modulus of elasticity for the concrete

\(\Delta \sigma_{pr}\) is the absolute value of the variation of stress in the tendons at location \(x\), at time \(t\), due to the relaxation of the prestressing steel; it is determined for a stress of \(\sigma_p = \sigma_p(G+P_{m0} + \psi_2 Q)\); where \(\sigma_p = \sigma_p(G+P_{m0} + \psi_2 Q)\) is the initial stress in the tendons due to initial prestress and quasi-permanent actions
\( \phi(t, t_0) \) is the creep coefficient at a time \( t \) and load application at time \( t_0 \).

\( \sigma_{c,\text{QP}} \) is the stress in the concrete adjacent to the tendons, due to self-weight and initial prestress and other quasi-permanent actions where relevant; the value of \( \sigma_{c,\text{QP}} \) may be the effect of part of self-weight and initial prestress or the effect of a full quasi-permanent combination of action \( (\sigma_c(G + P_{m0} + \psi_2 Q)) \), depending on the stage of construction considered.

\( A_p \) is the area of all the prestressing tendons at the location \( x \).

\( A_c \) is the area of the concrete section.

\( I_c \) is the second moment of area of concrete section.

\( z_{cp} \) is the distance between centre of gravity of the concrete section and tendons.
Prestressing force

The initial prestress force \( P_{m0}(x) \) at time \( t = t_0 \) applied to the concrete immediately after tensioning and anchoring (post-tensioning) or after transfer of prestressing (pre-tensioning)

\[
P_{m0}(x) = P_{\text{max}} - \sum \Delta P_i(x)
\]

where \( P_{\text{max}} \) is the force at tensioning

\[
(\sigma_{pm,\text{max}} = \min(0.80 f_{pk} ; 0.90 f_{p0,1k}))
\]

\( \Delta P_i(x) \) are the immediate losses

Limitation:

\( P_{m0}(x) \) should not exceed the following value

\[
P_{m0}(x) = A_p \cdot \sigma_{pm0}(x) \leq A_p \cdot \sigma_{pm0,\text{max}}
\]

where

\[
\sigma_{pm0,\text{max}} = \min(0.75 f_{pk} ; 0.85 f_{p0,1k})
\]
Immediate main losses of prestress for

a) pre-tensioning

During the stressing process:
- loss due to friction - in case of curved tendons $\Delta P_\mu(x)$
- losses due to wedge draw-in of the anchorage devices $\Delta P_w$

Before the transfer of prestress to concrete:
- loss due to relaxation of the pre-tensioning tendons (period between tensioning of tendons and transfer) $\Delta P_r$
- in case of heat curing, losses due to shrinkage and relaxation are modified; direct thermal effect should also be considered $\Delta P_T$

At the transfer of prestress to concrete:
- loss due to elastic deformation of concrete as the result of the action of pre-tensioned tendons when they are released from the anchorages $\Delta P_{el}$
a) post-tensioning

Short time losses:
- losses due to friction $\Delta P_\mu(x)$
- losses due to wedge draw-in of the anchorage devices $\Delta P_W$
- loss due to elastic deformation of concrete in case of sequential prestressing $\Delta P_{el}$
- loss due to bearing pressure on concrete – only by circumferential tendons with small radius of curvature
Long term losses

The mean value of the prestress force $P_{m,t}(x)$ at the time $t > t_0$ should be determined with respect to the prestressing method.

In addition to the immediate losses the time-dependent losses of prestress $\Delta P_{c+s+r}(x)$ as a result of creep and shrinkage of the concrete and the long term relaxation of the prestressing steel should be considered.

$$P_{m,t}(x) = P_{m0}(x) - \Delta P_{c+s+r}(x)$$